Adversarial Learning on Heterogeneous Information Networks

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ABSTRACT

Network embedding, which aims to represent network data in a low-dimensional space, has been commonly adopted for analyzing heterogeneous information networks (HIN). Although exiting HIN embedding methods have achieved performance improvement to some extent, they still face a few major weaknesses. Most importantly, they usually adopt negative sampling to randomly select nodes from the network, and they do not learn the underlying distribution for more robust embedding. Inspired by generative adversarial networks (GAN), we develop a novel framework HeGAN for HIN embedding, which trains both a discriminator and a generator in a minimax game. Compared to existing HIN embedding methods, our generator would learn the node distribution to generate better negative samples. Compared to GANs on homogeneous networks, our discriminator and generator are designed to be relation-aware in order to capture the rich semantics on HINs. Furthermore, towards more effective and efficient sampling, we propose a generalized generator, which samples "latent" nodes directly from a continuous distribution, not confined to the nodes in the original network as existing methods are. Finally, we conduct extensive experiments on four real-world datasets. Results show that we consistently and significantly outperform state-of-the-art baselines across all datasets and tasks.

CCS CONCEPTS

• Information systems → Data mining. • Computing methodologies → Learning latent representations.

KEYWORDS

Heterogeneous Information Network; Network Embedding; Generative Adversarial Network

1 INTRODUCTION

Network structures are ubiquitous in real-world applications, ranging from social and biological networks to transportation and telecommunication systems. Thus, network analysis is becoming increasingly important towards solving crucial problems such as personalized user recommendation on social networks [41] and disease gene identification on biological networks [2]. These problems often unfold as instances of node clustering, node classification and link prediction on network data, which fundamentally depend on an effective form of network representation. In recent years, network embedding [3, 8] has emerged as a promising direction for unsupervised learning of node representations, which aims to project the nodes of a network into a low-dimensional space whilst preserving the structural properties of the original network.

Heterogeneous information networks. While earlier network embedding work [14, 23] has attained considerable success, they can only cope with the so-called homogeneous networks, which comprise one single type of nodes and edges. However, in real-world scenarios, nodes naturally model different types of entity, which interact with each other through multiple relations. Such networks are known as Heterogeneous Information Networks (HIN) [28], as illustrated in Fig. 1(a) for bibliographic data. Observe that the toy HIN consists of multiple types of node (e.g., author and paper), which are connected by various types of relation (e.g., write/written relation between author and paper, and publish/published relation between paper and conference).

Due to its heterogeneity, HINs often carry immensely rich and complex semantics. Thus, more recent research has shifted towards HIN embedding, most notably Metapath2vec [11] and HIN2vec [12]. As shown in Fig. 1(b-1), existing HIN embedding methods fundamentally boil down to two samplers, which select "context" nodes from the network as positive (e.g., author $a_2$) and negative (the shaded circles) examples for a given "center" node (e.g., paper $p_2$), respectively. (Note that each node can serve as the center or context similar to the Skip-gram model [21].) Subsequently, a loss function is trained on these samples to optimize node representations. Although these methods have achieved some performance improvement, they suffer from serious limitations. First, they commonly utilize negative sampling to randomly select existing nodes in the network as negative samples. As such, their negative samples are not only arbitrary but also confined to the universe of the original
network. Second, they mainly focus on capturing the rich semantics on HINs without heeding to the underlying distribution of the nodes, and thus lack robustness for real-world HINs that are often sparse and noisy. Third, many HIN embedding methods [11, 26] rely on appropriate meta-paths to match the desired semantics, which typically require domain knowledge that is sometimes subjective and often expensive to obtain.

Adversarial learning. On another line, Generative Adversarial Networks (GAN) [13, 25] have been developed for learning robust latent representations in various applications [10, 35, 37]. GANs hinge on the idea of adversarial learning, where a discriminator and generator compete with each other to not only train a better discriminative model, but also learn the underlying data distribution. The latter makes the model more robust to sparse or noisy data [13, 24], and also provides better samples to reduce the labeling requirement. Given these advantages, there have been a few initial efforts on GAN-based network embedding [9, 22, 33, 38]. However, these studies only investigate homogeneous networks and thus do not account for the heterogeneity of nodes and edges, resulting in unsatisfactory performance on semantic-rich HINs.

Present work and challenges. Given the above limitations in current approaches, in this paper, we exploit the heterogeneity of HINs in an adversarial setting in order to learn semantic-preserving and robust node representations. However, its materialization is non-trivial, given two major challenges not addressed in existing GAN-based methods for homogeneous networks.

First, how to capture the semantics of multiple types of nodes and relations? In existing methods, real (i.e., positive) and fake (i.e., negative) nodes are only differentiated by network structure. Thus, it is imperative to design new forms of discriminator and generator that can differentiate and model real and fake semantic-rich nodes involved in various relations.

Second, how to generate fake samples efficiently and effectively? In existing methods, generators learn a finite discrete distribution over the nodes in a network. Thus, they often need to compute the intractable softmax function, and ultimately resort to approximations such as negative sampling [9] or graph softmax [33]. Moreover, they are essentially picking an existing node from the original network according to the learned distribution, without the ability to generalize to "unseen" nodes. Not surprisingly, they do not generate the most representative fake nodes, as such nodes may not even appear in the network. Thus, it is important to design a generator that can efficiently produce latent fake samples.

Insights and contributions. To address the above challenges, we propose HeGAN, a novel framework for HIN embedding with GAN-based adversarial learning. In particular, we propose a new form of discriminator and generator, as illustrated in Fig. 1(b-2). For the first challenge, our discriminator and generator are designed to be relation-aware in order to distinguish nodes connected by different relations. That is, w.r.t. any relation, the discriminator can tell whether a node pair is real or fake, whereas the generator can produce fake node pairs that mimic real pairs. In particular, a node pair is considered real only if (i) it is a positive pair based on network topology; and (ii) the pair is formed under the correct relation. For the second challenge, we design a generalized generator, which is able to directly sample latent nodes from a continuous distribution, such that (i) no softmax computation is necessary; and (ii) fake samples are not restricted to the existing nodes.

In summary, we make the following contributions.

(1) We are the first to employ adversarial learning for HIN embedding, in order to utilize the rich semantics on HINs. The solution is non-trivial due to the heterogeneity and the need for efficient and effective sample generation.

(2) We propose a novel framework HeGAN that is not only relation-aware to capture rich semantics, but also equipped with a generalized generator that is effective and efficient.

(3) We perform experiments on four public datasets on a series of downstream tasks. Results demonstrate that HeGAN consistently and significantly outperform various state-of-the-arts.

Figure 1: Overview of our work. (a) A toy example of HIN for bibliographic data. (b) Comparison between our work and previous works. (c) The framework of our proposed model HeGAN for adversarial learning on HINs.
Table 1: Summary of notations

<table>
<thead>
<tr>
<th>Notion</th>
<th>Explanation</th>
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<tr>
<td>( \mathcal{G} )</td>
<td>a heterogeneous information network (HIN)</td>
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<tr>
<td>( \mathcal{V}, \mathcal{E} )</td>
<td>the set of node and edges, resp.</td>
</tr>
<tr>
<td>( \mathcal{A}, \mathcal{R} )</td>
<td>the set of node and edge types, resp.</td>
</tr>
<tr>
<td>( e^G, e^D )</td>
<td>node embedding of generator and discriminator, resp.</td>
</tr>
<tr>
<td>( M^G, M^D )</td>
<td>relation matrix of generator and discriminator, resp.</td>
</tr>
<tr>
<td>( \theta^G, \theta^D )</td>
<td>parameters of generator and discriminator, resp.</td>
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2 PRELIMINARY

In this section, we formalize the problem of HIN embedding and introduce the background on GAN. Main notations are summarized in Table 1, including those to be introduced in Sect. 3.

HIN embedding. Our study focuses on heterogeneous information networks [28], which can be defined as follows.

**Definition 1.** Heterogeneous information network (HIN). A HIN \( \mathcal{G} = (\mathcal{V}, \mathcal{E}, \mathcal{A}, \mathcal{R}, \phi, \varphi) \) is a form of graph, where \( \mathcal{V} \) and \( \mathcal{E} \) denote the sets of nodes and edges, respectively. It is also associated with a node type mapping function \( \phi : \mathcal{V} \rightarrow \mathcal{A} \) and an edge type mapping function \( \varphi : \mathcal{E} \rightarrow \mathcal{R} \), where \( \mathcal{A} \) and \( \mathcal{R} \) denote the sets of node and edge types such that \( |\mathcal{A}| + |\mathcal{R}| > 2 \).

An example of HIN is illustrated in Fig. 1(a) on bibliographic data. Observe that it consists of multiple node types (e.g., author, paper, conference and term) and their semantic relations (e.g., author–write–paper, paper–contain–term).

The goal of HIN embedding is to learn a mapping function to project each node \( v \in \mathcal{V} \) to a low-dimensional space \( \mathbb{R}^d \), where \( d \ll |\mathcal{V}| \). Node representations in the new space should preserve not only the structure, but also the rich semantics on the HIN.

Generative adversarial networks. Our work is inspired by the recent success of GANs, which can be viewed as a minimax game between two players, namely, generator \( G \) and discriminator \( D \), in the following manner.

\[
\min_{\theta^G} \max_{\theta^D} \quad \mathbb{E}_x \text{-} P_{data} \left[ \log D(x; \theta^D) \right] + \mathbb{E}_{z \sim P_z} \left[ \log \left( 1 - D(G(z; \theta^G); \theta^D) \right) \right].
\]  

The generator \( G \) tries to generate fake samples as close to the true data as possible with the noise \( z \) from a predefined distribution \( P_z \), where \( \theta^G \) denotes the parameters of the generator. On the contrary, the discriminator \( D \) aims to distinguish real data from the distribution \( P_{data} \) and fake data from the generator, where \( \theta^D \) denotes the parameters of the discriminator. In practice, GAN has been found [25] to often work better if the generator minimizes \( -\log D(G(z; \theta^G)); \theta^D) \) instead of \( \log \left( 1 - D(G(z; \theta^G); \theta^D) \right) \).

3 THE PROPOSED APPROACH: HeGAN

In this section, we present the proposed model HeGAN, a novel HIN embedding approach based on GAN. We begin with the overall framework, followed by elaborations on our discriminator and generator. Lastly, we discuss the optimization of our framework, as well as comparison to other models.

3.1 Overall Framework of HeGAN

As shown in Fig. 1(c), our framework mainly consists of two competing players, the discriminator and the generator. Given a node, the generator attempts to produce fake samples associated with the given node to feed into the discriminator, whereas the discriminator tries to improve its parameterization to separate the fake samples with the real ones actually connected to the given node. The better trained discriminator would then force the generator to produce better fake samples, and the process is repeated. During such iterations, both the generator and discriminator receives mutual, positive reinforcement. While this setup may appear similar to previous efforts [4, 9, 22, 33, 38] on GAN-based network embedding, we employ two major novelties to address the challenges of adversarial learning on HINs.

First, existing studies only leverage GAN to distinguish whether a node is real or fake w.r.t. structural connections to a given node, without accounting for the heterogeneity in HINs. For example, given a paper \( p_2 \), they treat nodes \( a_2, a_4 \) as real, whereas \( a_1, a_3 \) are fake simply based on the topology of the HIN shown in Fig. 1(a). However, \( a_2 \) and \( a_4 \) are connected to \( p_2 \) for different reasons: \( a_2 \) writes \( p_2 \) and \( a_4 \) only views \( p_2 \). Thus, they miss out on the valuable semantics carried by HINs, unable to differentiate \( a_2 \) and \( a_4 \) even though they play distinct semantic roles. Towards semantic-preserving embedding, we introduce a relation-aware discriminator and generator, to differentiate various types of semantic relation between nodes. On our toy HIN, given a paper \( p_2 \) as well as a relation, say, write/rewrite, our discriminator is able to tell apart \( a_2 \) and \( a_4 \), and our generator will try to produce fake samples more similar to \( a_2 \) instead of \( a_4 \).

Second, existing studies are limited in sample generation in both effectiveness and efficiency. They typically model the distribution of nodes using some form of softmax over all nodes in the original network. In terms of effectiveness, their fake samples are constrained to the nodes in the network, whereas the most representative fake samples may fall “in between” the existing nodes in the embedding space. For example, given a paper \( p_2 \), they can only choose fake samples from \( \mathcal{V} \), such as \( a_1 \) and \( a_3 \). However, both may not be adequately similar to real samples such as \( a_2 \). Towards a better sample generation, we introduce a generalized generator that can produce latent nodes such as \( a' \) shown in Fig. 1(c), where it is possible that \( a' \notin \mathcal{V} \). For instance, \( a' \) could be the “average” of \( a_1 \) and \( a_3 \) and is more similar to the real sample \( a_2 \). In terms of efficiency, the softmax function is expensive to compute, and approximations such as negative sampling and Graph Softmax must be employed. In contrast, our generator can sample fake nodes directly without using a softmax.

3.2 Discriminator and Generator in HeGAN

In the ensuing discussion, we shall zoom into the proposed discriminator and generator for HeGAN.

3.2.1 Relation-aware discriminator. As motivated, on a HIN it is imperative to distinguish real and fake nodes under a given relation. Thus, our relation-aware discriminator \( D(v; u, r; \theta^D) \) evaluates the connectivity between the pair of nodes \( u \) and \( v \) w.r.t. a relation \( r \). Specifically, \( u \in \mathcal{V} \) is a given node and \( r \in \mathcal{R} \) is a given relation from the HIN \( \mathcal{G} \), \( v \) is the embedding of a sample node \( v \) (which
can be real or fake), and $\theta^D$ denotes the model parameters of $D$. In essence, $D$ outputs a probability that the sample $v$ is connected to $u$ under the relation $r$. We quantify this probability as:

$$D(e_v(u, r; \theta^D)) = \frac{1}{1 + \exp \left(-e_v^T \mathbf{M}^D_r e_u^r\right)}.$$ (2)

where $e_u \in \mathbb{R}^{d \times 1}$ is the input embedding of the sample $u$, $e_v^D \in \mathbb{R}^{d \times 1}$ is the learnable embedding of node $u$, and $\mathbf{M}^D_r \in \mathbb{R}^{d \times d}$ is a learnable relation matrix for relation $r$. $\theta^D = \{e_u^D : u \in V, \mathbf{M}^D_r : r \in R\}$ form the model parameters of $D$, i.e., the union of all node embeddings and relation matrices learnt by $D$.

Naturally, the probability should be high when $v$ is a positive sample related to $u$ through $r$, or low when it is a negative sample. In general, a sample $v$ form a triple $(u, v, r)$ together with the given $u$ and $r$, and each triple belongs to one of the three cases below with regard to its polarity. Each case also contributes to one part of the discriminator’s loss, inspired by the idea of conditional GAN [25].

**Case 1: Connected under given relation.** That is, nodes $u$ and $v$ are indeed connected through the right relation $r$ on the HIN $G$, such as $(a_2, p_2, \text{write})$ shown in Fig. 1(a). Such a triple is considered positive and can be modeled by the below loss.

$$L^D = \mathbb{E}(u, v, r) - \log D(e_v(u, r | \theta^D)).$$ (3)

Here we draw the positive triple from the observed $G$, denoted as $(u, v, r) \sim P_G$.

**Case 2: Connected under incorrect relation.** That is, $u$ and $v$ are connected in the HIN under a wrong relation $r' \neq r$, such as $(a_2, p_2, \text{view})$. The discriminator is expected to mark them as negative, too, as their connectivity does not match the desired semantics carried by the given relation $r$. We define this part of loss as follows.

$$L^D = \mathbb{E}(u, v, r') - \log (1 - D(e_v(u, r'))).$$ (4)

Here, we still draw the pair of nodes $(u, v)$ from $G$, but the negative relation $r'$ is drawn from $R' = R \setminus \{r\}$ uniformly.

**Case 3: Fake node from relation-aware generator.** That is, given a node $u \in V$, it can form a fake pair with the node $v$ supplied by the generator $G(u, r; \theta^G)$, such as $(a', p_2, \text{write})$ in Fig. 1(c). As we shall see later in Sect. 3.2.2, the generator is also relation-aware: it attempts to generate a fake node’s embedding that mimics the real nodes connected to $u$ under the correct relation $r$. Again, the discriminator aims to identify this triple as negative, which can be formulated as follows.

$$L^D = \mathbb{E}(u, r) - \log (1 - D(e_v(u, r | \theta^G))).$$ (5)

Note that the fake sample $v$’s embedding $e'_v$ is drawn from the generator $G$’s learnt distribution. As we shall see in Sect. 3.2.2, it is distinct from $G$'s own model parameters $\theta^G$. On the other hand, the discriminator $D$ simply treats $e'_v$ as non-learnable input, and only optimizes its own parameters $\theta^D$.

It is worth noting that, arguably there could be a fourth case, where the triple is a fake pair from a relation-oblivious generator. However, such negative triples are believed to be more easily separated from the positives than the negatives in Case 2 or 3. Thus, we do not consider them here, although our model is flexible to incorporate this fourth case.

We integrate the above three parts to train the discriminator:

$$L^D = L^D_1 + L^D_2 + L^D_3 + \lambda^D ||\theta^D||^2_2,$$ (6)

where $\lambda^D > 0$ controls the regularization term to avoid overfitting. The parameters $\theta^D$ of the discriminator can be optimized by minimizing $L^D$.

**3.2.2 Relation-aware, generalized generator.** The goal of our generator $G(\cdot; \theta^G)$ is to generate fake samples to mimic the real one. On the one hand, $G$ is relation-aware just as the discriminator. Thus, given a node $u \in V$ and a relation $r \in R$, the generator $G(u, r; \theta^G)$ aims to generate a fake node $v$ likely to connect to $u$ in the context of relation $r$. In other words, $v$ should be as close as possible to a real node, say, $w$ such that $(u, w, r) \sim P_G$. On the other hand, our generator is generalized, which means the fake node $v$ can be latent and not found in $V$.

To meet the two requirements, our generator should also employ relation-specific matrices (for relation-awareness), and generate samples from an underlying continuous distribution (for generalization). In particular, we leverage the following Gaussian distribution:

$$N(e_u^G, M_u^G, \sigma^2I),$$ (7)

where $e_u^G \in \mathbb{R}^{d \times 1}$ and $M_u^G \in \mathbb{R}^{d \times d}$ denote the node embedding of $u \in V$ and the relation matrix of $r \in R$ for the generator. In other words, it is a Gaussian distribution with mean $e_u^G$ and covariance $\sigma^2I$ as choices of $\sigma$. Intuitively, the mean represents a fake node likely to be connected to $u$ by relation $r$, and the covariance represents potential deviations. One naive solution is to directly generate samples from $N(e_u^G, M_u^G, \sigma^2I)$. Nevertheless, as neural networks have shown strong ability in modeling complex structure [15], we integrate the multi-layer perceptron (MLP) into the generator for enhancing the expression of the fake samples. Hence, our generator is formulated as follows,

$$G(u, r; \theta^G) = f(W_L \cdot f(W_I e + b_I) + b_L),$$ (8)

where we draw $e$ from the distribution $N(e_u^G, M_u^G, \sigma^2I)$. Here $W_L$ and $b_L$, respectively denote the weight matrix and the bias vector for each layer, and $f$ is an activation function. The parameter set of the generator is thus $\theta^G = \{e_u^G : u \in V, M_u^G : r \in R, W, b\}$, i.e., the union of all node embeddings and relation matrices, as well as the parameters of MLP.

As motivated earlier, the generator wishes to fool the discriminator by generating close-to-real fake samples, such that the discriminator gives high score to them. The generator aims to optimize $\theta^G$ of the generator can be optimized by minimizing $L^G$:

$$L^G = \mathbb{E}(u, r) - \log D(e_v(u, r | \theta^G)) - \log D(e_v(u, r | \theta^G)) + \lambda^G ||\theta^G||^2_2,$$ (9)

where $\lambda^G > 0$ controls the regularization term. The parameters $\theta^G$ of the generator can be optimized by minimizing $L^G$.

**3.3 Optimization and Complexity Analysis**

We adopt the iterative optimization strategy to train HeGAN. In each iteration, we alternate the training between the generator and discriminator. Specifically, we first fix $\theta^G$, and generate fake samples to optimize $\theta^D$ and thus improve the discriminator. Next, we fix $\theta^D$, and optimize $\theta^G$ in order to produce increasingly better fake samples as evaluated by the discriminator. We repeat the above
Algorithm 1: Model training for HeGAN

Require: HIN $G$, number of generator and discriminator trainings per epoch $n_G$, $n_D$, number of samples $n_s$
1: Initialize $\theta_G$ and $\theta_D$ for $G$ and $D$, respectively
2: while not converge do
3:     for $n = 0; n < n_G$ do
4:         Discriminator training
5:             Sample a batch of triples, i.e., $(u, v, r) \sim P_G$
6:             Generate $n_s$ fake nodes $e' \sim G(u; r; \theta_G)$ for each $(u, r)$
7:         end for
8:     for $n = 0; n < n_D$ do
9:         Generator training
10:        Sample a batch of triples, i.e., $(u, v, r) \sim P_G$
11:       Generate $n_s$ fake nodes $e' \sim G(u; v; \theta_G)$ for each $(u, v)$
12:      end for
13:     end while
14: return $\theta_G$ and $\theta_D$

We now conduct a complexity analysis. The updating of the generator and discriminator in each iteration mainly involve the updating of node vectors and relation matrices, whose time complexity is $O(n_s \cdot |V| \cdot d^2)$, where $n_s$ is the number of samples, $|V|$ is the number of nodes and $d$ is the embedding dimensionality. Hence, the complexity of training our model per iteration is $O((n_G + n_D) \cdot n_s \cdot |V| \cdot d^2)$, where $n_G$ and $n_D$ are the number of generator and discriminator training per iteration, respectively. Since we treat $n_G$, $n_D$, $n_s$ and $d$ as small constants, the complexity of each iteration in our model is linear with the number of nodes in the HIN, i.e., $|V|$, indicating the efficiency and scalability of HeGAN.

4 EXPERIMENTS

In this section, we evaluate the effectiveness of HeGAN on a wide range of tasks, including node clustering and classification, as well as link prediction and recommendation. We further analyze the model performance in the contexts of the underlying mechanism, efficiency and parameter sensitivity.

4.1 Experimental Setup

4.1.1 Datasets. We conduct extensive experiments on four benchmark datasets [12, 15], namely DBLP (with four types of nodes: author, paper, conference and term), Yelp (user, business, service, star and reservation), AMiner (author, paper, conference and reference), and Movielens (user, movie, age, occupation and type). We organize them into HINs, as summarized in Table 2. On the first three datasets, we perform node classification and clustering w.r.t. the given labels, as well as link prediction. Movielens is reserved for a recommendation task. Task descriptions will be postponed until their respective experiments.

4.1.2 Baselines. We consider three categories of network embedding methods: traditional (Deepwalk, LINE), GAN-based (GraphGAN, ANE) and HIN (HERec-HNE, HIN2vec, Metapath2vec) embedding algorithms.

- **Deepwalk** [23] performs truncated random walks on networks, and employs the skip-gram model.
- **LINE** [31] exploits the first (LINE-1st) and second (LINE-2nd) order proximity in networks.
- **GraphGAN** [33] unifies generative and discriminative learning with GAN in a minimax game.
- **ANE** [9] adopts the adversarial learning principle to push the latent representations towards a fixed posterior distribution.
- **HERec-HNE** [27] designs a type-constrained strategy to filter node sequences for semantic-preserving HIN embedding.
- **HIN2vec** [12] learns latent representations of both nodes and meta-paths jointly, and thus preserves the semantics of HINs.

4.1.3 Implementation. Working details, including hyperparameter settings, will be discussed in the reproducibility supplement. We will also study the impact of hyperparameters in HeGAN in Sect. 4.3.4.

4.1.4 Significance Test. For tabular results in Tables 3, 4 and 5, we use ** (or *) to indicate that HeGAN is significantly different from the runner-up method based on paired $t$-tests at the significance level of 0.01 (or 0.05).

4.2 Experimental Analysis

In this section, we empirically compare HeGAN and the baselines on various downstream tasks. Note that we do not report the results of GraphGAN on the AMiner dataset, since it cannot run on this large dataset even on a machine with 256GB memory.

4.2.1 Node Clustering. We employ the K-Means algorithm to perform clustering, and evaluate the clustering quality in terms of normalised mutual information (NMI) w.r.t. the node labels.
Based on the results in Table 3, we make the following observations. (i) HeGAN is consistently better than all the baselines, demonstrating its effectiveness for learning representations in HINs. (ii) Among the baselines, HIN embedding methods (i.e., HERec-HNE, HIN2vec and Metapath2vec) generally outperform traditional methods, implying the importance of semantic-preserving embedding. (iii) HeGAN significantly outperforms both HIN and GAN-based (i.e., ANE and GraphGAN) embedding methods, showing that our model can learn semantic-preserving representations in a robust manner through the adversarial principle. Overall, HeGAN achieves performance gains over the best baseline by 3%, 10% and 6% on the three datasets, respectively.

4.2.2 Node Classification. We use 80% of the labeled nodes to train a logistic regression classifier, and test the classifier on the remaining 20% nodes.

Since the tasks are multi-class, we report Macro-F1, Micro-F1 and Accuracy on the test set in Table 4. Similar conclusions to the node clustering task can be drawn, where HeGAN consistently outperforms the best baseline with statistical significance. It is also worth noting that our performance margins over the best baseline are smaller compared to the node clustering task, since in classification all methods are helped by the supervision, narrowing their gaps.

4.2.3 Link Prediction. In this task, we predict user-business links on Yelp, and author-paper links on DBLP and AMiner. We randomly hide 20% of such links from the original network as the ground truth positives, and randomly sample disconected node pairs of the given form as negative instances. The ground truth serves as our test set. Subsequently, we utilize the residual network to learn node representations. After obtaining the node representations, we adopt two ways to perform link prediction, namely, logistic regression and inner product. To train the logistic regression classifier, we used links and negative instances from the residual network without overlapping with the test set.

Since this is a binary task, we adopt Accuracy, AUC and F1 as evaluation metrics, as shown in Table 5. Again, similar conclusions can be drawn, where HeGAN consistently and significantly outperforms all the baselines, except for one case. We further observe that, the performance lead of HeGAN over the best baseline is much larger with inner product than with logistic regression. In particular, in terms of F1 scores, with inner product we outperform the best baseline by 6%, 7% and 11% on the three datasets, respectively, whereas with logistic regression the improvement is only about 2%. We hypothesize that HeGAN innately learns a much better structure- and semantics-preserving embedding space than the baseline methods, since the inner product only relies on the learned representations without resorting to any external supervision.

4.2.4 Recommendation. We adopt the Movielens dataset for the recommendation task. For each user, we aim to recommend a set of unseen movies which may be liked by the user. Following [15], we adopt the leave-one-out method for evaluation, i.e., the last movie of each user is held out for testing, and the remaining data are used for training the node embeddings. During testing, we select top-K movies with the highest inner product with the target user, and evaluate the recommendation performance with HR@K (hit ratio) and NDCG@K.

We report the results of HeGAN and three representative baselines, namely, Deepwalk, GraphGAN and Metapath2vec. From Fig. 2, we observe that HeGAN consistently outperforms all the baselines across all K values on both evaluation metrics. For example, HeGAN outperforms the baselines by 41%~106% in HR@10, and 44%~126% in NDCG@10. This task shows the effectiveness of HeGAN on a ranking-based objective. It is worth noting that Metapath2vec is not performing well in this task. One hypothesis is that there is a lack of meaningful meta-paths in the Movielens dataset.

4.2.5 Network Visualization. To examine the network representations intuitively, we visualize the embeddings of business nodes in Yelp using the t-SNE [20] algorithm in Fig. 3. From the plots,
Table 5: Performance comparison on link prediction. (bold: best; underline: runner-up)

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| Regression | Deepwalk | 0.5474 | 0.7231 | 0.6874 | 0.5654 | 0.8164 | 0.6953 | 0.5309 | 0.6064 | 0.6799 |
| Regression | LINE-1st | 0.6647 | 0.7753 | 0.7363 | 0.6769 | 0.7832 | 0.7199 | 0.6113 | 0.6899 | 0.7123 |
| Regression | LINE-2nd | 0.4728 | 0.4797 | 0.6325 | 0.4193 | 0.7347 | 0.5909 | 0.5000 | 0.4785 | 0.6666 |
| Regression | GraphGAN | 0.5218 | 0.6543 | 0.6023 | 0.5432 | 0.7425 | 0.6324 | 0.5421 | 0.6123 | 0.6663 |
| Regression | ANE | 0.5332 | 0.6825 | 0.6214 | 0.5702 | 0.7725 | 0.6894 | - | - | - |
| Regression | HERec-HNE | 0.5123 | 0.7473 | 0.6878 | 0.5323 | 0.6756 | 0.7066 | 0.6063 | 0.6912 | 0.6798 |
| Regression | HIN2vec | 0.5775 | 0.8295 | 0.6714 | 0.6273 | 0.8340 | 0.4194 | 0.5348 | 0.6934 | 0.6824 |
| Regression | Metapath2vec | 0.4775 | 0.6926 | 0.6287 | 0.5124 | 0.6324 | 0.6702 | 0.6243 | 0.7123 | 0.6953 |
| Regression | HeGAN | 0.7649** | 0.8712** | 0.7837** | 0.7391** | 0.8298 | 0.7705** | 0.6505** | 0.7431** | 0.7752** |

Figure 3: Visualization of representative baselines and HeGAN on Yelp. Color indicates the category of business.

Figure 4: Learning curves of HeGAN on Yelp.
Figure 5: Impact of heterogeneity and generalized generator.

Figure 6: Efficiency evaluation on three datasets. (a) Time per generator training in log scale. (b) Overall training in log scale. (c) Scalability w.r.t. the number of nodes ($\times 10^3$) in linear scale.

different types of nodes and relations in HINs should be distinguished, as disregarding such information leads to the worse performance of HeGAN-hete compared to HeGAN. Second, between HeGAN-hete and GraphGAN, as both do not utilize heterogeneous information, their key difference lies in their generators. In particular, our model is generalized, in the sense that it generates fake, potentially latent, samples from a continuous Gaussian distribution, whereas GraphGAN generates only pick fake nodes from the original network. The result shows that our generalized generator can indeed produce more representative samples.

4.3.3 Efficiency. As mentioned above, our generalized generator draws samples directly from a continuous distribution, which significantly accelerates the training of generators. In contrast, GraphGAN employs Graph Softmax in its generator—although it is much more efficient than the normal softmax, it is not as fast as the generator of HeGAN. We report the updating time per generator training and per overall training epoch in Fig. 6(a) and (b), respectively. As shown, HeGAN runs about ten times faster than GraphGAN for both generator and overall training, demonstrating that our generator is not only effective, but also efficient. (Note that GraphGAN cannot run on AMiner due to memory constraint.)

We also conduct a scalability study, by sampling a few smaller sub-networks from AMiner. The results are shown in Fig. 6(c), where the running time of HeGAN increases linearly w.r.t. the number of nodes, consistent with our complexity analysis in Sect. 3.3.

4.3.4 Parameter Analysis. Finally, we investigate the impact of the parameters in the following categories, using the node clustering quality as a reference. Similar patterns have been observed on the performance of other tasks.

First, the number of generator and discriminator training per epoch, $n_G$ and $n_D$. They control the balance between the two players. We run a grid search over $(1, 5, 10, 15, 20)^2$ and plot their performance in Fig. 7(a). HeGAN achieves the optimal performance near $(5, 15)$, i.e., $n_G = 5, n_D = 15$. In general, the performance is stable when the discriminator is trained more than the generator, i.e., when $n_D \geq 10$ and $n_G \leq 10$. This observation is consistent with previous findings [1].

Second, the embedding dimension, $d$. As shown in Fig. 7(b), overall our model is not sensitive to this parameter. Nevertheless, the optimal performance is obtained when $d$ is 64 or 128.

Third, the variance of Gaussian distribution, $\sigma^2$. As shown in Fig. 7(c), our model achieves optimal performance when $\sigma^2 = 1.0$ and is generally stable around that value, although too small or large values (such as $\sigma^2 < 0.1$) would harm the model.

5 RELATED WORK

We review the most related work in network embedding, HIN embedding and generative adversarial networks.

Network embedding. Network embedding [3, 8] has shown its potential to learn structure-preserving node representations, and has been successfully applied to many data mining tasks. Contemporary methods usually explore network topology as context information, based on random walks (e.g., Deepwalk [23] and node2vec [14]), neighborhoods (e.g., LINE [31] and SDNE [32]) or high-order proximity (i.e., GraRep [5], NEU [36] and AROPE [40]). Unfortunately, these methods only deal with homogeneous networks, and thus they cannot learn semantic-preserving representations in HINs. Meanwhile, recently emerged graph neural networks (e.g., GCN [18]) are proposed for representation learning in an end-to-end manner with task-specific supervision. Their goals differ from our scope, which aims to learn node presentations in an unsupervised manner to support arbitrary downstream tasks.

HIN embedding. Recently, heterogeneous information networks (HIN) [28] have been proposed to model complex entities and their rich relations in various applications [7, 16, 17, 27, 34, 39]. To marry the advantages of HIN and network embedding, numerous methods [11, 26, 29, 30] have been proposed for representation learning in HINs. One major line of work leverages meta-path-based contexts for semantic-preserving embedding, including meta-path-based similarity [26] and meta-path-based neighbors [11]. Note that these methods rely on domain knowledge to choose the right meta-paths, whereas there also exist a few methods [6, 12, 29, 30] which do not require meta-path selection. Moreover, task-specific embedding learning in HINs [7, 27, 34] has also been explored recently, which
departs from our goal to learn structure- and semantic-preserving representations to support arbitrary tasks.

**Generative adversarial networks.** Generative adversarial networks (GANs) [13] have demonstrated superior performance in many problems [19, 35, 37]. They hinge on the principle of adversarial learning, where a generator and discriminator compete with each other to improve their outcomes. Inspired by GANs, a few studies [4, 9, 22, 33, 38] leverage the adversarial principal to learn more robust representations. Some of them [4, 9, 22, 38] impose a fixed prior distribution on the embedding space to enhance the robustness of the learned representations. However, these methods ignore the heterogeneity of nodes and relations, and thus cannot capture the rich semantics on HINs.

**6 CONCLUSION**

In this paper, we proposed a novel framework called HeGAN for HIN embedding based on the adversarial principle. We elaborately designed the relation-aware discriminator and generator to fit the heterogeneous setting. Specifically, w.r.t. to a given relation, the discriminator can tell whether a node pair is real or fake, whereas the generator can produce fake node pairs that mimic real pairs. To further improve the effectiveness and efficiency of sample generation, we proposed a generalized generator, which is able to directly sample latent nodes from a continuous distribution. Expensive experimental results have verified the effectiveness and efficiency of HeGAN on various tasks.

**7 ACKNOWLEDGEMENTS**

This research was supported by the National Natural Science Foundation of China (No. 61772082, 61702296), the National Key Research and Development Program of China (2017YFB0803094), the Singapore National Research Foundation (4182043) and the Singapore Ministry of Education (MOE) Academic Research Fund (AcRF) Tier 1 grant (Approval No. 18-C220-SMU-006).

**REFERENCES**

[29] Yu Shi, Huan Gui, Qi Zhu, Lance Kaplan, and Jiawei Han. 2018. AspEm: Embedding Learning by Aspects in Heterogeneous Information Networks. In SDM. 144–152.
[34] Hongwei Wang, Fuzheng Zhang, Min Hou, Xing Xie, Minyi Guo, and Qin Liu. 2018. SHINE: signed heterogeneous information network embedding for sentiment link prediction. In WSDM. 592–600.
A IMPLEMENTATION DETAILS

A.1 Environment
We implement the proposed model using the Python library TensorFlow. All the experiments are conducted on a Linux server with one GPU (GeForce RTX) and CPU (Intel Xeon W-2133). We release the source code of HeGAN at https://github.com/librahu/HeGAN. And the data in the paper is available at https://github.com/librahu/HIN-Datasets-for-Recommendation-and-Network-Embedding.

A.2 Parameter Settings for HeGAN
We perform Adaptive Moment Estimation (Adam) to optimize our model with learning rate 0.0001. Moreover, we set the regularization parameters for the generator and discriminator to $\lambda_D = \lambda_G = 0.0001$, and utilize a two-layer MLP with a ReLU activation function for the generator. For each iteration of generator and discriminator training, we use a batch size of 32 and set the number of samples to $n_s = 16$. We run $n_G = 5$ iterations of generator training and $n_D = 15$ iterations of discriminator training in each epoch. Careful initialization of neural network model is crucial to avoid poor local minima. Hence, HeGAN initializes initial embeddings in generator and discriminator from a pretrained embedding model (Metapath2vec).

A.3 Parameter Settings for Baselines
The embedding dimensions for all methods are set as 64. For random walk-based methods (i.e., Deepwalk, HIN2vec and Metapath2vec), we set the number of walks per node to $w = 10$, the walk length to $l = 100$ and the window size to $\tau = 5$. For HIN embedding methods (i.e., HERec-HNE and Metapath2vec), we select the meta-paths APCPA, UBStBU, APCPA and UMTMU in DBLP, Yelp, AMiner and Movielens, respectively, since they have the best performance under these meta-paths. For LINE, we set the number of samples as 10000. For GraphGAN, we set the learning rate as 0.001 and the number of samples as 20. For ANE, we follow the parameter settings in the original paper.

1https://www.tensorflow.org/